

EENG 426/CPSC 459/ENAS 876

Silicon Compilation

Specifying Algorithms: Communicating Hardware Processes

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Communicating Hardware Processes

CHP = Communicating Hardware Processes

(based on Tony Hoare's CSP language)

CSP = Communicating Sequential Processes

- Assignment-based (imperative)
- No memory allocation
- No variable declaration (only shared/local)

Not a complete programming language.

Sequential part

skip statement that does nothing.

$x := E$ assignment statement

$x := \mathbf{true} \quad \equiv \quad x \uparrow$

$x := \mathbf{false} \quad \equiv \quad x \downarrow$

$x := a \vee b$

$x := c \wedge \neg d$

$y := y + 1$

Operationally:

- evaluate expression on the RHS
- assign the result of evaluation to the variable

Sequential part

Arrays are really an address-calculation mechanism.

$$\begin{aligned}dmem[addr] &:= x \\ ins &:= imem[pc]\end{aligned}$$

Only use arrays when absolutely necessary!

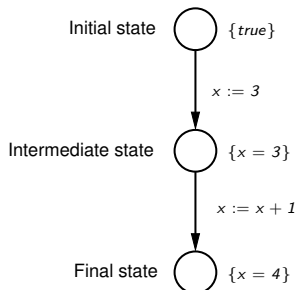
Bit-fields are useful for extracting part of a variable

$$reg[ins_{31..27}] := reg[ins_{26..22}] + reg[ins_{21..17}]$$

Sequential Composition:

$$S_1; S_2$$

Execute statement 1. Then execute statement 2.



Control structures: selection

Selection Statement: Used to choose between different alternatives, like an IF statement.

Deterministic selection:

$$\begin{array}{l} [G_1 \longrightarrow S_1 \\ \quad [G_2 \longrightarrow S_2 \\ \quad \quad \dots \\ \quad \quad [G_n \longrightarrow S_n \\ \quad] \\] \end{array}$$

Wait for one G_i to be true. Execute corresponding S_i .

Restriction: Atmost one guard can be true.

Control structures: selection

Non-deterministic selection Statement:

$$\begin{array}{l} [G_1 \longrightarrow S_1 \\ | G_2 \longrightarrow S_2 \\ | \dots \\ | G_n \longrightarrow S_n \\] \end{array}$$

More than one G_i can be true. Pick one.

Standard abbreviation:

$$[B] \equiv [B \longrightarrow \mathbf{skip}]$$

Examples

What do the following programs do?

$$\begin{array}{l} [\text{true} \longrightarrow x\uparrow \\ | \text{true} \longrightarrow x\downarrow \\] \end{array}$$
$$[xi]; xo\uparrow; [\neg xi]; xo\downarrow$$
$$\begin{array}{l} [x = 1 \longrightarrow y := 3 \\ [] x = 2 \longrightarrow y := 5 \\ [] x = 3 \longrightarrow y := 7 \\] \end{array}$$

Control structures: loops

Loops: Repeat actions while conditions are satisfied. A generalization of the WHILE loop.

Deterministic loop:

$$\begin{array}{l} * [G_1 \longrightarrow S_1 \\ \quad \square G_2 \longrightarrow S_2 \\ \quad \square \dots \\ \quad \square G_n \longrightarrow S_n \\] \end{array}$$

At most one G_i can be true. Repeatedly execute until all guards are false.

Control structures: loops

Non-deterministic loop:

$$\begin{array}{l} * [G_1 \longrightarrow S_1 \\ \quad | G_2 \longrightarrow S_2 \\ \quad | \dots \\ \quad | G_n \longrightarrow S_n \\] \end{array}$$

More than one G_i can be true.

Standard abbreviation:

$$* [S] \equiv * [\mathbf{true} \longrightarrow S]$$

Examples

Add integers from one to ten:

```
i := 1;  
sum := 0;  
*[i ≤ 10 → sum := sum + i; i := i + 1]
```

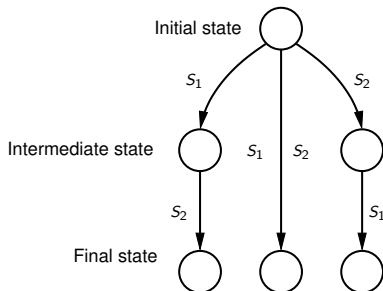
Euclid's algorithm:

```
{X > 0 ∧ Y > 0}  
x, y := X, Y;  
*[x > y → x := x - y  
  [x < y → y := y - x  
  ]  
  ]  
{x = gcd(X, Y)}
```

Parallel composition:

$$S_1 \parallel S_2$$

Execute statements 1 and 2 in parallel.



What is the net effect of:

$$1. x := 1 \parallel y := 2$$

$$2. x := 1 \parallel x := 2$$

$$3. x := x + 1 \parallel x := 3$$

($x = 0$ initially)

$$1. x = 1 \wedge y = 2$$

Postulate: Concurrent activities of programs that do not share variables do not interfere with each another.

We're assuming a perfect physical world. Some effects that we're ignoring include:

- charge-sharing
- cross-talk
- ground bounce

Therefore, we have to ensure that these effects are in fact negligible!

2. *Software* : $x = 1 \vee x = 2$

Hardware : $x = 1 \vee x = 2 \vee \text{bad stuff}$

3. *Software* : $x = 1 \vee x = 3 \vee x = 4$

Hardware : $x = 1 \vee x = 3 \vee x = 4 \vee \text{bad stuff}$

No atomicity postulate for writing variables!!!

We use arbiters to solve the problem of interference.

When designing hardware, our task is to implement (in one form or another) the atomicity assumption that is commonly made by software!

What is the net effect of:

$$4. x\uparrow \parallel y := x$$

$$5. x\uparrow \parallel [x]; y := x$$

$$6. *[x\uparrow; x\downarrow] \parallel *[y\uparrow; y\downarrow]$$

$$7. *[x\uparrow; x\downarrow] \parallel *[[x]; y\uparrow; y\downarrow]$$

(initially x and y are false)

4. x

5. $x \wedge y$

Postulate: Reading a single boolean-valued variable is an atomic action.

Implementing such a read is tricky in the case when the variable being read is being modified at the same time. The implementation of such a read uses a synchronizer.

6. *infinite execution*

Postulate (weak fairness): We assume that actions from both processes get a chance to execute eventually. If an action from a process can execute, it will get to execute eventually.

7. *infinite execution*

In this case, it is possible that only a finite number of changes to y occur.

An action must be enabled and stay enabled for it to get a chance to execute.

CPU example

```
*[(i, pc) := (imem[pc], pc + 1);  
  [offset(i.op) → (offset, pc) := imem[pc], pc + 1  
  [] ¬offset(i.op) → skip  
  ];  
  [alu(i.op) → (reg[i.z], f) := aluf(reg[i.x], reg[i.y], i.op, f)  
  [] ld(i.op) → reg[i.z] := dmem[reg[i.x] + reg[i.y]]  
  [] st(i.op) → dmem[reg[i.x] + reg[i.y]] := reg[i.z]  
  [] ldx(i.op) → reg[i.z] := dmem[offset + reg[i.y]]  
  [] stx(i.op) → dmem[offset + reg[i.y]] := reg[i.z]  
  [] lda(i.op) → reg[i.z] := offset + reg[i.y]  
  [] stpc(i.op) → reg[i.z] := pc + reg[i.x]  
  [] jmp(i.op) → pc := reg[i.y]  
  [] brch(i.op) → [cond(f, i.cc) → pc := pc + offset  
                  [] ¬cond(f, i.cc) → skip  
                ]  
  ]]
```